



# Sunspot number, group number and $F_{10.7}$ : new insights

Frédéric Clette, Laure Lefèvre, Shreya Bhattacharya

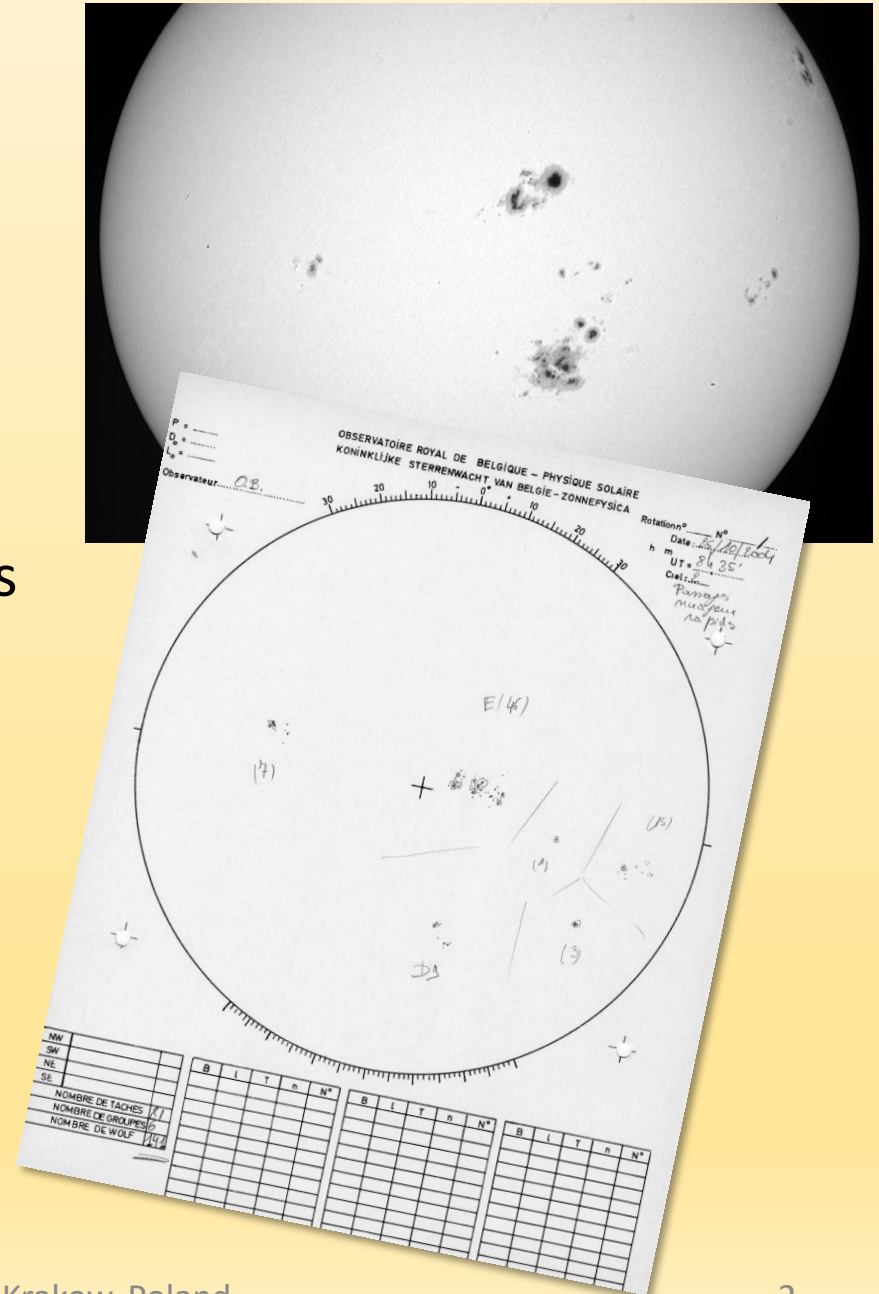
World Data Center SILSO

Royal Observatory of Belgium, Brussels



# Outline


- Sunspot and Group number: the differences
- Sunspot number recalibration
- Group number reconstructions
- Benchmarks and proxies
- A byproduct: revisiting the  $F_{10.7}$  index
- Conclusions



# Introduction: two sunspot number time series

## Sunspot Number

$$S_N = 10 N_g + N_s$$

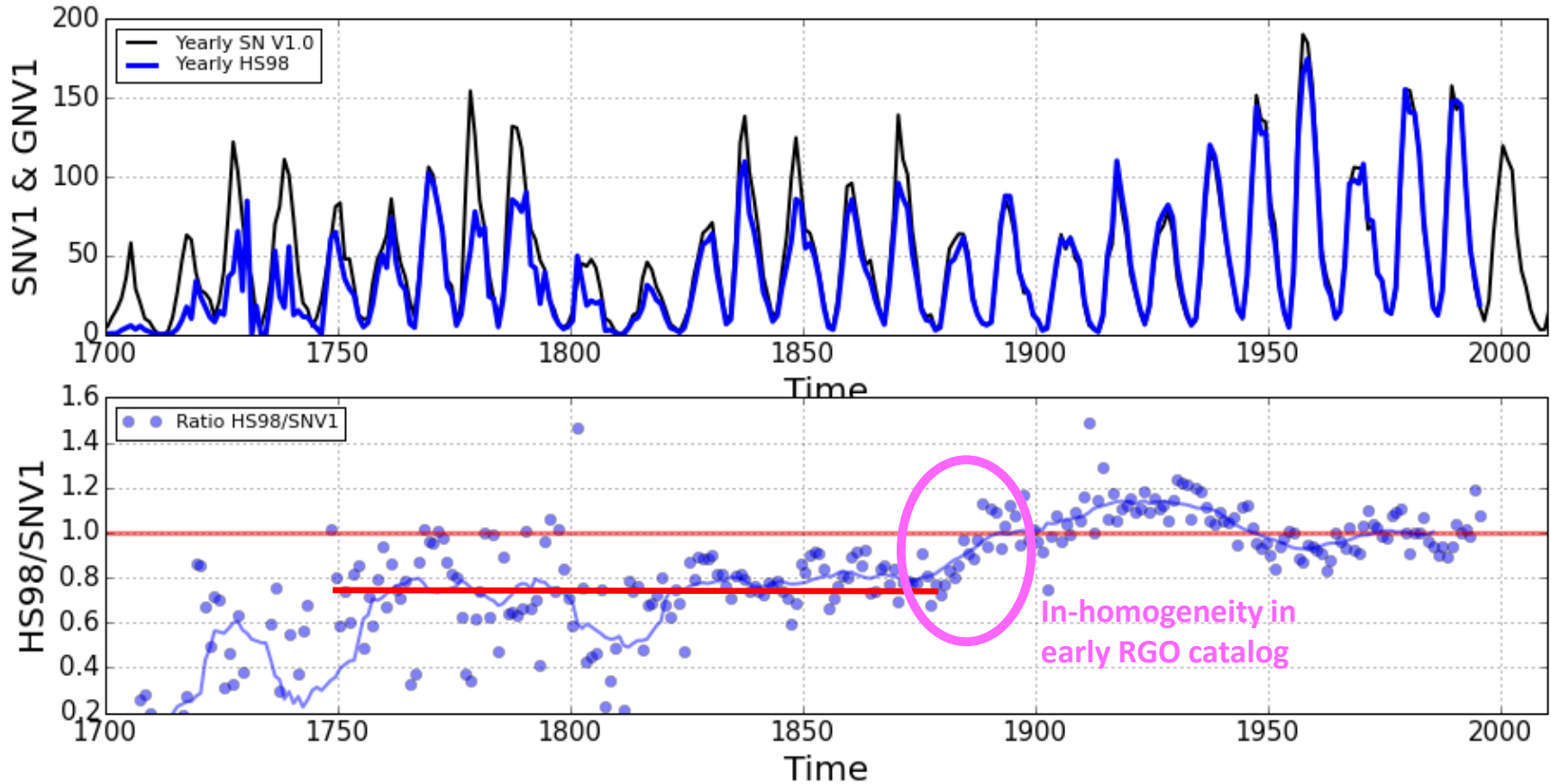
- Origin: R. Wolf (1849)
- Start: 1700 (end of Maunder minimum)
- Continuous production to present
- Production in 3 parts: 
  - **1700-1849**: reconstruction from historical documents
  - **1849-1980**: Zurich Observatory
  - **1981-now**: World Data Center SILSO, Brussels
- Calibration:
  - **Pilot station: Zurich Observatory**
    - Successive primary observers
    - Specola Observatory **Locarno** (since 1981)
  - Standard telescope, trained observers

## Sunspot group number

$$G_N = 20.13 N_g$$

- Origin: Hoyt and Schatten (1998)
- Start: 1610 (telescope)
- End: 1995 (paper publication)
- Production:
  - Single recent reconstruction
  - Based on an **extended set of raw historical data**
- Calibration:
  - “Daisy-chaining” of observers backwards in time
  - Starting reference: **Royal Greenwich Observatory photographic catalog (1875-1975)**

# SN introduction: a primordial disagreement



- **Very good match after 1900**
- **Large disagreement before the 20<sup>th</sup> century:  $G_N$  lower than  $S_N$  by up to 40%**

# Recalibration effort

- Community effort started in Sept. 2011
- **4 Sunspot Number Workshops**
  - Renewed interest for the  $S_N$
  - Several new reconstructions

## Synthesis in:

- **Solar Physics:** Topical Issue « Recalibration of the Sunspot Number», **Volume 291 9-10, 2016**, Eds. Clette, Cliver, Lefèvre, Vaquero, Svalgaard, **35 articles**

- **ISSI Team 2018-2022:**

*([www.issibern.ch/teams/sunspotnoser/](http://www.issibern.ch/teams/sunspotnoser/))*

- Work on new SN version (V3)
- Steps to a continuous “update – QC – vetting” process (IAU framework)
- **Focused topical collaborations**

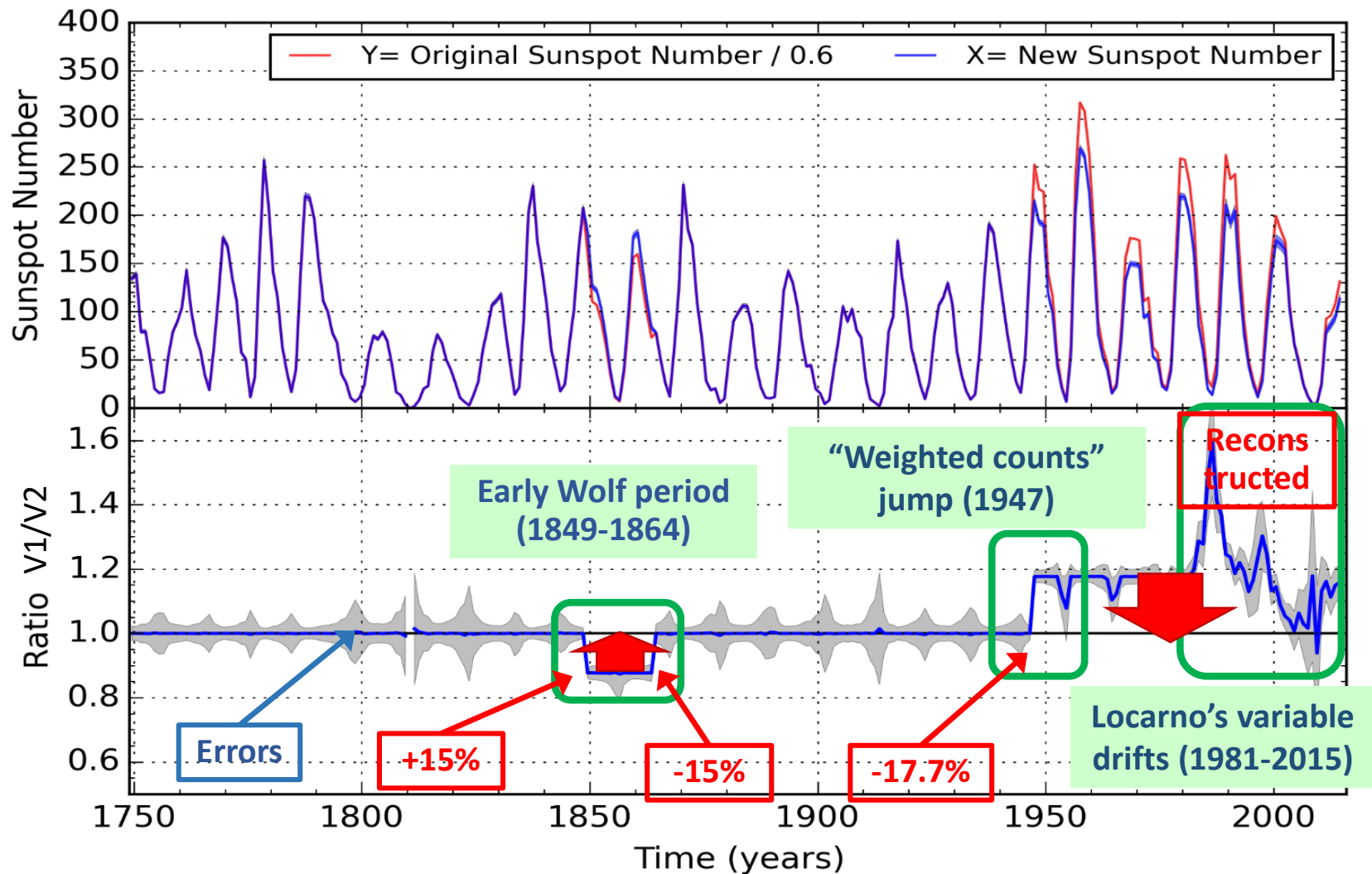


NSO, Sac Peak,  
USA, Sept. 2011



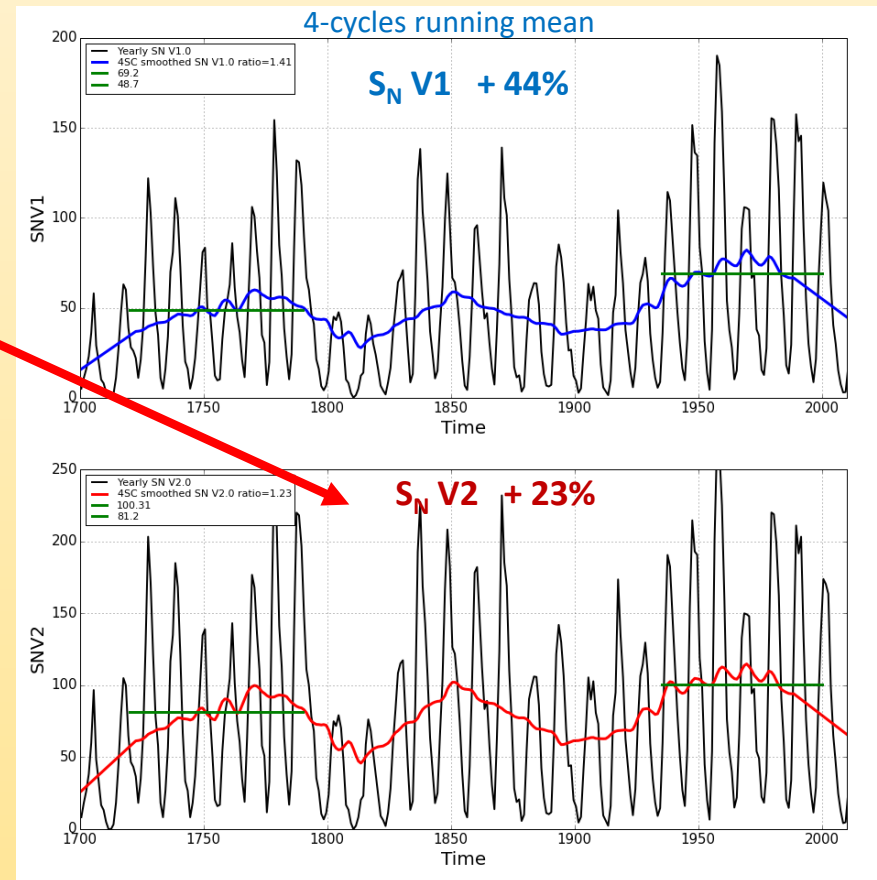
ISSI Bern, Switzerland  
Jan. 2018

# $S_N$ revision: version 2.0 (release: July 2015)



# Why does it matter? Diverse impacts

- **Past solar forcing on climate:**
  - Nature of grand minima: onset and exit?
  - Nature of grand maxima: no higher amplitude, but longer duration of high sequence
- **Constraints on dynamo models**
- **Mid and long-term forecasts**
- **$S_N$ - $G_N$  proxies put recent solar measurements in a long-term context:**
  - Reconstitution of past irradiance, solar wind, etc. (e.g. SATIRE)
- **Calibration reference for solar, geomagnetic and ionospheric proxies**

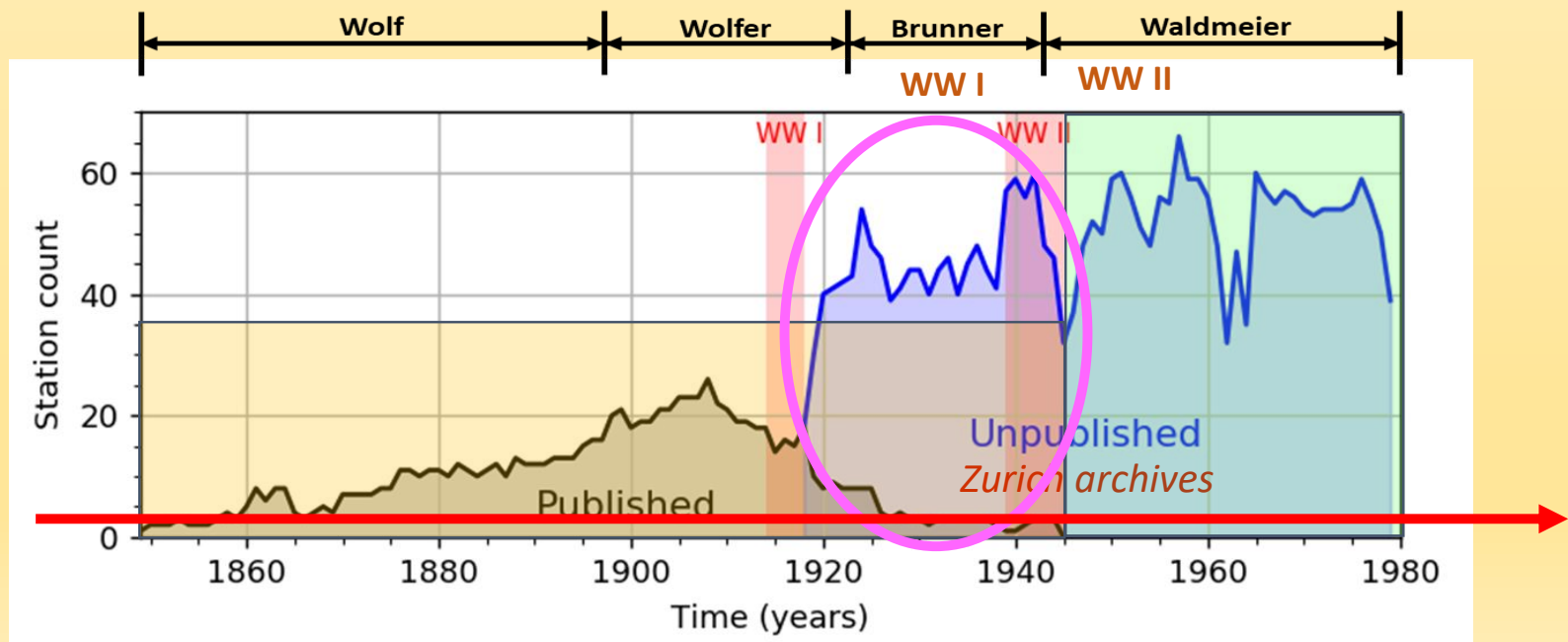




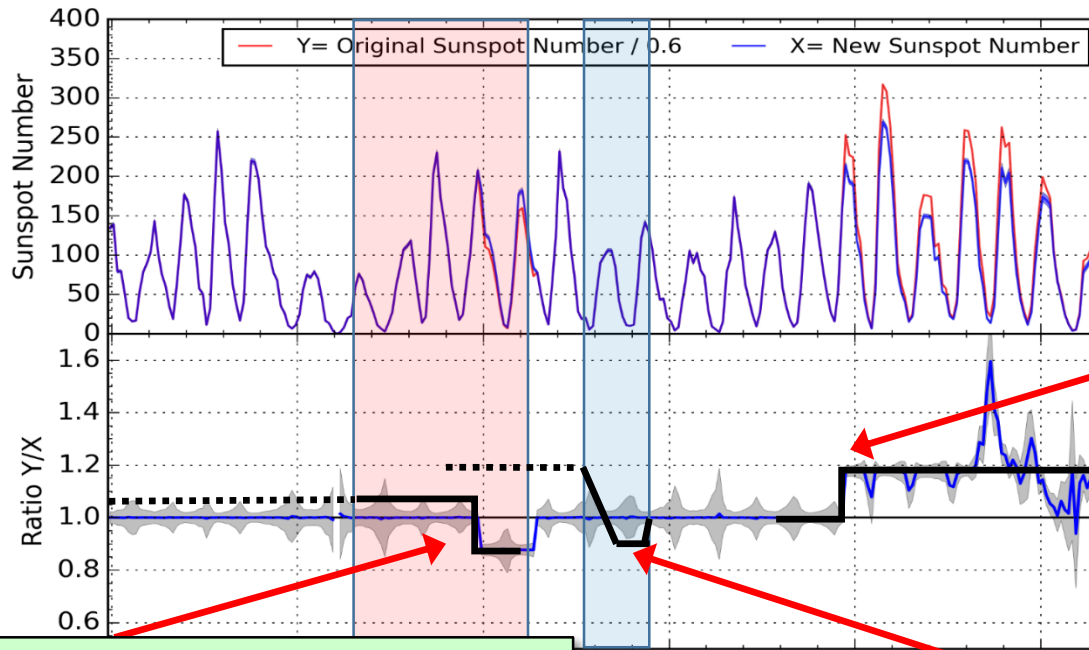


# $S_N$ database: major advances *(Clette et al. 2020)*

- **All published input data from Zurich** (*Astronomische Mittheilungen der Sternwarte Zurich*):
    - Fully digitized up to 1944 (internal and auxiliary observers)
  - Unpublished data (archives) 1919- 1980:
    - **Original sourcebooks recovered: all source data between 1945 and 1970**
      - Scanned by the Library & Archives of ETH Zurich (2019-2021)
      - Extraction of all values (~300.000) in preparation (FARSUN brain.be project, 2023)
- ➔ **Full continuity up to 1980 (transition to SILSO, Brussels)**
- **Still partly missing: auxiliary data 1919-1944**



# $S_N$ ongoing corrections



**1947 jump +17.7 %**  
*Clette et al. 2021*

- Global agreement on jump amplitude
- Variable inflation factor 1-1.2
- Timing of jump explained: sharp break in Zurich team and network

**Schwabe - Wolf -20%**  
*Bhattacharya et al. 2022*

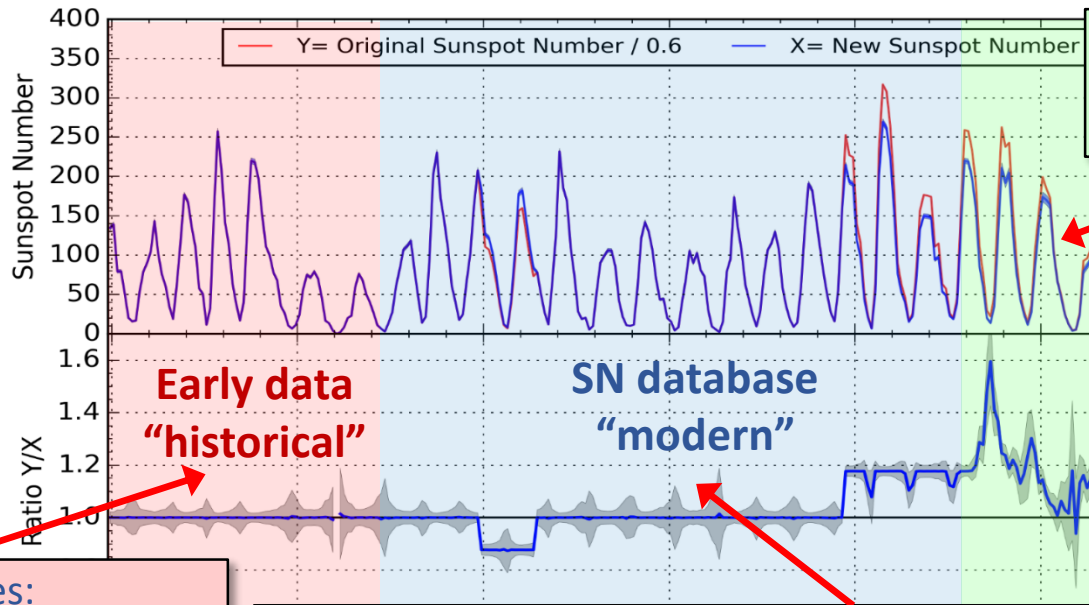
- Past hints: Leussu et al.(2013), Senthamizh et al. (2015)
- Data: Interval 1818-1868

**Wolf - Wolfer -20% ?**  
*Friedli 2020*

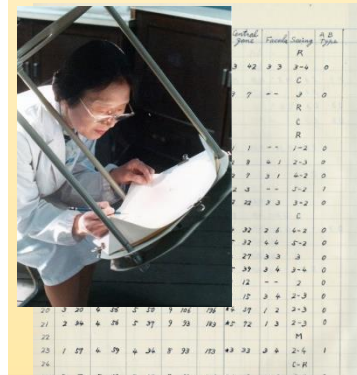
- Work by E.Frenkel (1913) revisited

- **All recent papers: productive COVID period !**
- **Most corrections = abrupt transitions**
  - Are corrections applicable to all earlier data?
  - No slow drifts between jump? (stability of primary reference observers)

# $S_N$ : towards a full end-to-end $S_N$ reconstruction



**2015 reconstruction**  
*Clette & Lefèvre 2016*  
 • Already in SN V2.0



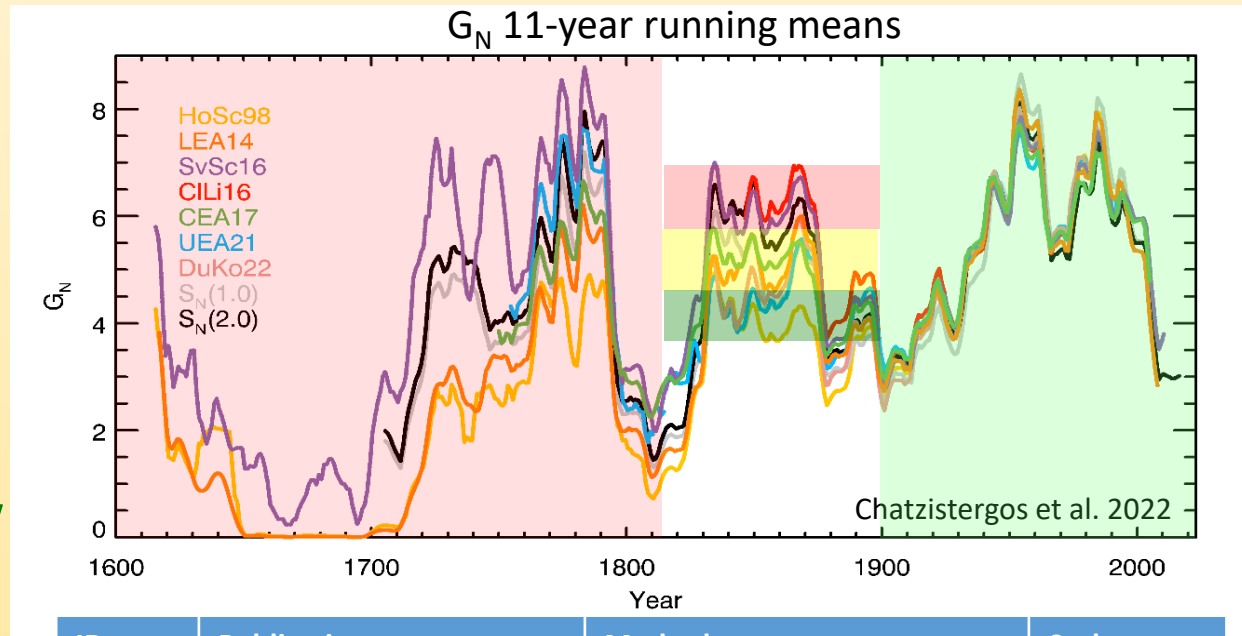
- Challenging issues:
  - Sparse data
  - No clear distinction between spots and groups
- Role of sunspot drawings!
  - Allows recounting
  - Statistics of individual
- Overview of data

- $S_N$  Database (all Zurich records):
  - Waldmeier archives (FARSUN project, SILSO, late 2023)
- Adding new and revised data sets:
  - Carrington 1853-1861 (*Bhattacharya, Teague, 2022*)
  - Madrid 1935-1986 (*Aparicio et al. 2018, 2022*)
  - I. Koyama 1945-1986 (*Hayakawa et al. 2020*)
  - + recovery of still-missing Zurich archives 1919-1944?
- Inclusion of uncertainties; data mining techniques

**Time consuming part: data encoding (> 300 000 values)**  
**V2.1/2.2** (Schwabe-Wolf-Wolfer corrections) > **2023** (Bhattacharya PhD)  
**V3.0** (full reconstruction back to 1818) > **2024-2025** (FARSUN)

# $G_N$ revision: multiple series

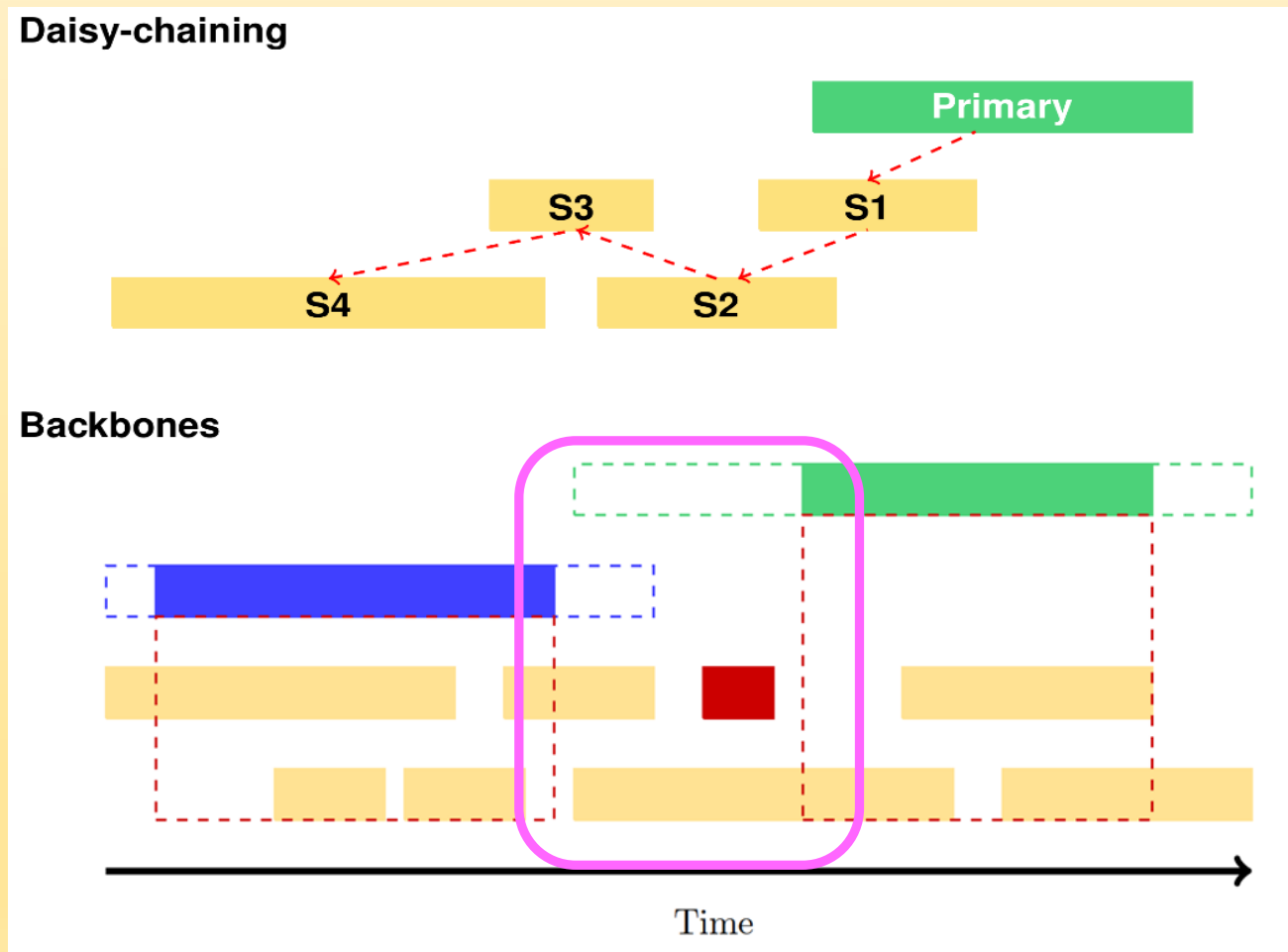
- 10-year smoothed series (*Chatzistergos*)
- 7  $G_N$  series:
  - Range (19<sup>th</sup> century): 40%
  - 3 rough classes: **high**, **medium**, **low**



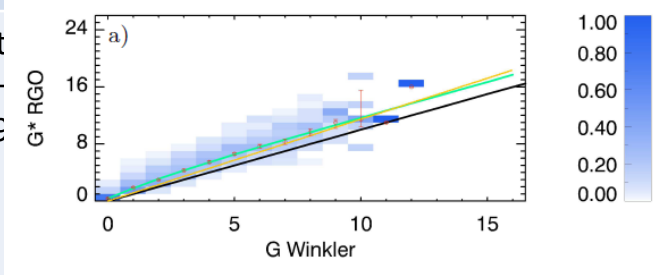
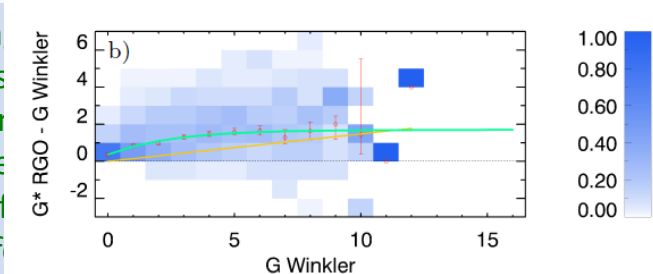
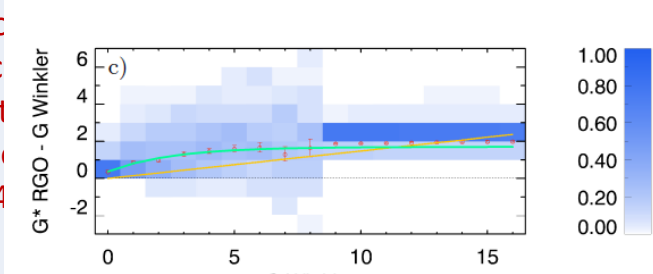
- Before the 19<sup>th</sup> century:
  - Large uncertainties
  - Simple propagation of 19<sup>th</sup> century scaling

ID	Publication	Method	Scale
<i>SN(1.0)</i>	<i>Zurich (original)</i>	<i>SN, pilot station</i>	<i>High</i>
HoSc98	Hoyt & Schatten 1998	GN orig., daisy-chain	Low
LEA14	Lockwood et al. 2014	H&S GN-based SN correction	Med-Low
<i>SN(2.0)</i>	<i>Clette et al. 2016</i>	<i>SN(1.0) corrected, pilot station</i>	<i>High</i>
SvSc16	Svalgaard & Schatten 2016	Backbone 1	High
CLi16	Cliver & Ling 2016	HoSc98 correction, daisy-chain	High
CEA17	Chatzistergos et al. 2017	Backbone 2	Med-High
UEA21	Usoskin et al. 2016, 2021	Active-day fraction	Med-Low
DoKo22	Dudok de Wit 2022	Tied ranking	Med-Low

# $G_N$ methods: daisy-chaining versus backbones

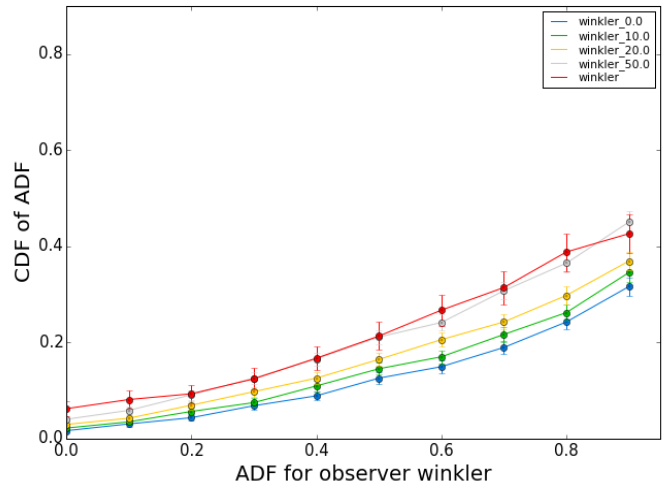


# $G_N$ methods: Observer-pair comparison

	Cliver & Ling 2016	Svalgaard & Schatten 2016	Chatzistergos et al. 2017
<b>Method</b>	<ul style="list-style-type: none"> <li>Daisy-chaining</li> </ul>	<ul style="list-style-type: none"> <li>Backbone</li> </ul>	<ul style="list-style-type: none"> <li>Advanced backbone</li> </ul>
<b>Innovations</b>	<ul style="list-style-type: none"> <li>Crit of H of 199</li> </ul>		<ul style="list-style-type: none"> <li>More primary observers</li> <li>No temporal averaging (daily values)</li> <li>Corrections through cross-probability distributions (non-parametric CPD)</li> </ul>
<b>Assets</b>	<ul style="list-style-type: none"> <li>Direct overlap between primary observers</li> <li>Allows non-linear relations between observer pairs</li> <li>Error estimate</li> </ul>		<ul style="list-style-type: none"> <li>Direct overlap between primary observers</li> <li>Allows non-linear relations between observer pairs</li> <li>Error estimate</li> </ul>
<b>Issues</b>	<ul style="list-style-type: none"> <li>Lack of data at high <math>G_N</math> values (Monte-Carlo simulation)</li> <li>Observers assumed to be global CPD</li> </ul>		<ul style="list-style-type: none"> <li>Lack of data at high <math>G_N</math> values (Monte-Carlo simulation)</li> <li>Observers assumed to be global CPD</li> </ul>
<b>Result</b>	<ul style="list-style-type: none"> <li>High</li> </ul>	<ul style="list-style-type: none"> <li>Highest</li> </ul>	<ul style="list-style-type: none"> <li>Intermediate</li> </ul>

**Most mature  $G_N$  reconstruction !**

# $G_N$ methods: Observer-pair comparison

	Usoskin et al. 2016, 2021 Willamo et al. 2017, 2018	Muñoz-Jaramillo (preliminary)	Dudok de Wit & Kopp (2022, in preparation)
<b>Method</b>	<ul style="list-style-type: none"> <li>Active-day fraction (ADF)</li> </ul>	<ul style="list-style-type: none"> <li>Segmented ADF</li> </ul>	<ul style="list-style-type: none"> <li>Tied ranking</li> </ul>
<b>Innovations</b>	<ul style="list-style-type: none"> <li>Statistics of days with <math>G_N=0</math> and <math>G_N &gt; 0</math></li> <li>Single “perfect” observer (RGO 1900-1976)</li> <li>Degraded data: <math>S_5</math> minimum area threshold (acuity)</li> </ul>	<ul style="list-style-type: none"> <li>Objective selection of</li> </ul>	<ul style="list-style-type: none"> <li>Ranking of <math>G_N</math> values</li> </ul>
<b>Assets</b>	<ul style="list-style-type: none"> <li>No observer-pair comparisons</li> <li>Non-parametric correction (RGO-based) via cross-probability distribution (CPD)</li> <li>Error estimate</li> </ul>	<ul style="list-style-type: none"> <li>Bias</li> </ul>	
<b>Issues</b>	<ul style="list-style-type: none"> <li>Bias when different activity levels between RGO and observer (<i>Willamo et al. 2018</i>)</li> <li>Unreported spotless days</li> <li>Effect of group splitting (beyond acuity factor)</li> <li>Works only when <math>ADF &lt; 0.8</math></li> </ul>	<ul style="list-style-type: none"> <li>In values next to pure ADF</li> </ul>	<ul style="list-style-type: none"> <li>No understanding (yet) of the mutual influence of gap-filling and ranking steps.</li> </ul>
<b>Result</b>	<ul style="list-style-type: none"> <li>Medium-low</li> </ul>	<ul style="list-style-type: none"> <li>No series yet</li> </ul>	<ul style="list-style-type: none"> <li>Medium-low</li> </ul>

**Not yet fully validated!**

# $G_N$ reconstruction: archive of source data

- Updated  $G_N$  database (Vaquero et al. 2016):

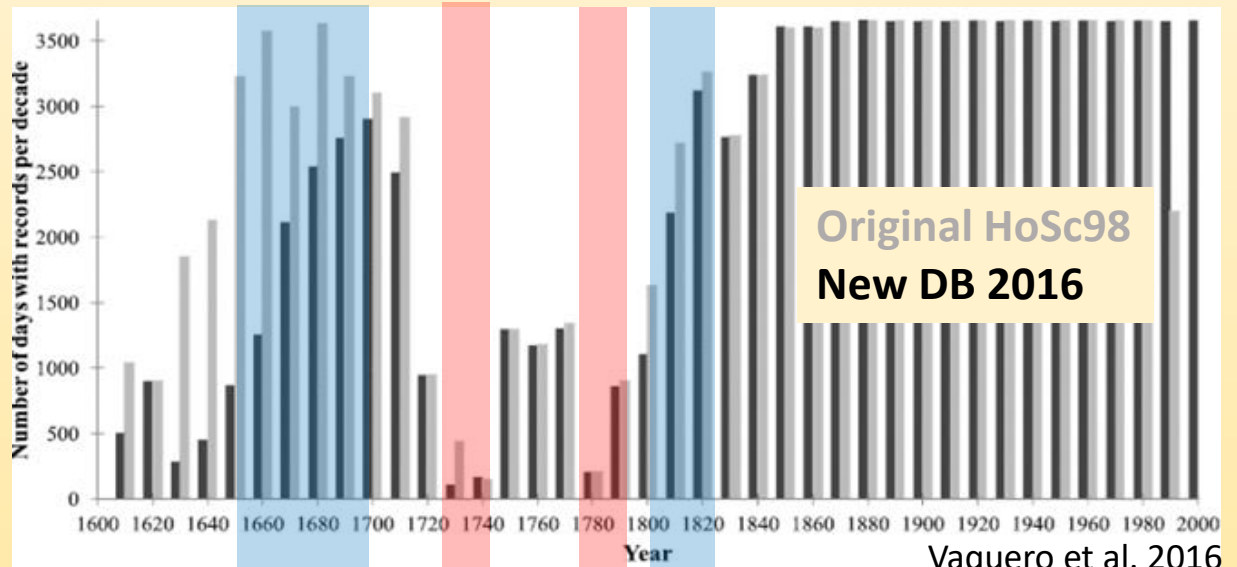
- Additions
- Corrections
- Eliminations

- Main gaps in 18<sup>th</sup> century:

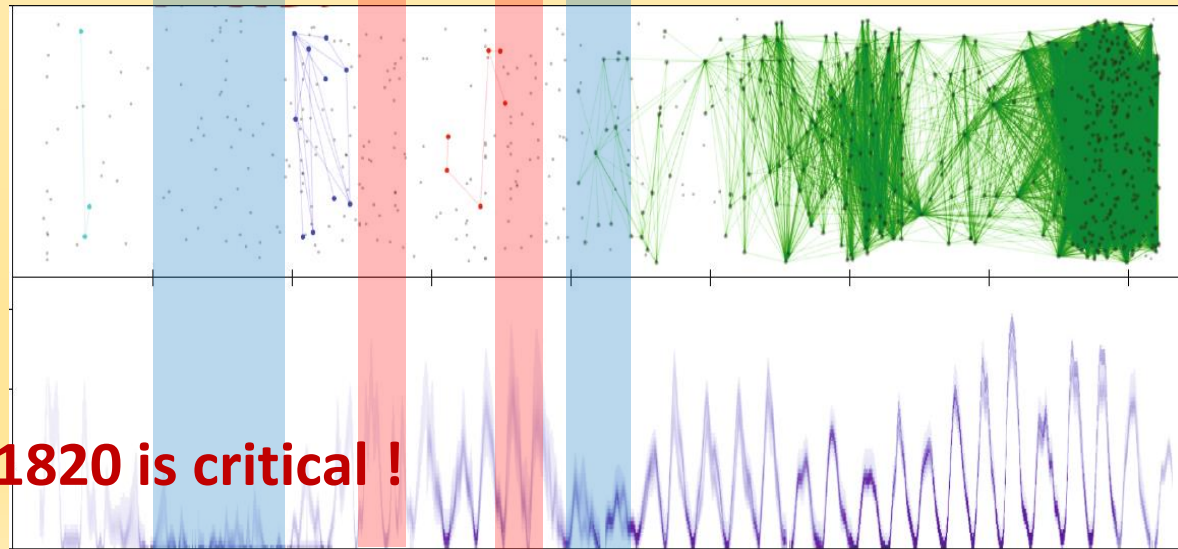
- 1740-1750
- 1780 – 1800

- Major spotless periods:

- 1650 – 1715 (Maunder)
- 1800-1820 (Dalton)



Vaquero et al. 2016



Muñoz-Jaramillo, Vaquero 2018

➔ Adding data before 1820 is critical !



# GN-SN data: intensive recoveries !

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[https://doi](https://doi.org/10.3847/1538-4357/abdd34)

THE ASTROPHYSICAL JOURNAL, 909:194 (7pp), 2021 March 10  
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<https://doi.org/10.3847/1538-4357/abdd34>

## Thaddäus Derfflinger's Sunspot Observations during 1802–1824: A P

	1610 -1699	1700-1799	1800-1899	1900 - 1999
Hisa				
<sup>1</sup> G <sup>2</sup> UK Solar Sy	T. Harriot 1610-1613 C. Scheiner 1611-1631 J. Tardé 1615-1617	Plantade 1705-1726 P. Becker 1708-1710 J-H. Müller 1709	T. Derfflinger 1802-1824 Prantner 1804-1844 F. Hallaschka 1814-1816	Madrid 1876-1986 Stonyhurst Coll. 1886-1940
THE ASTROPHYSICAL © 2021. The American	C. Malapert 1618-1626 C. Scheiner ~1620	J-C Müller 1719-1720 J.F. Weidler 1728-1729	H. Schwabe 1825-1867 A. Colla 1830-1843	M. Aguilar 1914-1920 Coimbra Obs 1929-1941
Sunspot C	Derham ~1620	P. Wargentin 1747	Kunitomo 1835-1836	R. Carrasco 1931-1933
Hisashi	J. Smogulecki 1621-1625	J.C. Staudacher 1749-1796	W.C. Bond 1847-1849	H. Koyama 1945-1996
<sup>1</sup> Institute f <sup>3</sup> UK Solar System	D. Mögling 1626-1629 P. Gassendi ~1630	C. Horrebow 1761-1776	R. Carrington 1853-1861 G. Spoerer 1861-1894	E. Strach 1969-2008
	G. Marcgraf 1636-1642	Japan 1749-1750	A. Secchi 1871-1875	
<sup>7</sup> Rea	Rheita 1642	B. Oriani 1778-1779		
Solar Phy <a href="https://c">https://c</a>	Hevelius 1642-1645	Toaldo 1779		
	M. Fogelius 1650-1700	Comparetti 1779		
	H. Siverus 1650-1700	I. Zenbei 1793		
	Cassini 1671	Armagh Obs. 1795-1797		
Anal (161!	J-C. Gallet 1677			
	G. Kirch 1680-1709			
	Eimmart Obs. 1681-1718			
v.M.S.	J. Flamsteed 1672-1703			

H. Hayakawa<sup>2,3,7,8</sup> 

r M.S. Carrasco<sup>7</sup>  · Bruno P. Besser<sup>8,9</sup>  · Shoma Uneme<sup>2</sup> · Shinsuke Imada<sup>2</sup> 

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Laboratory,

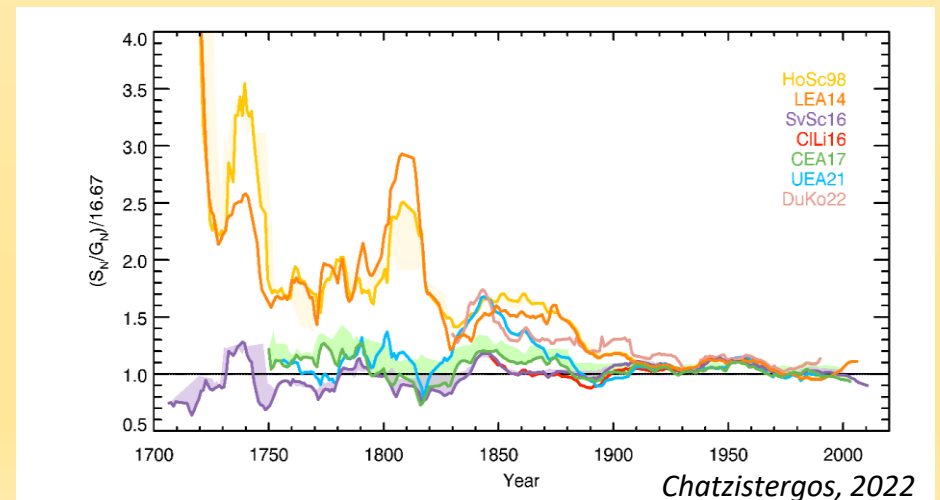
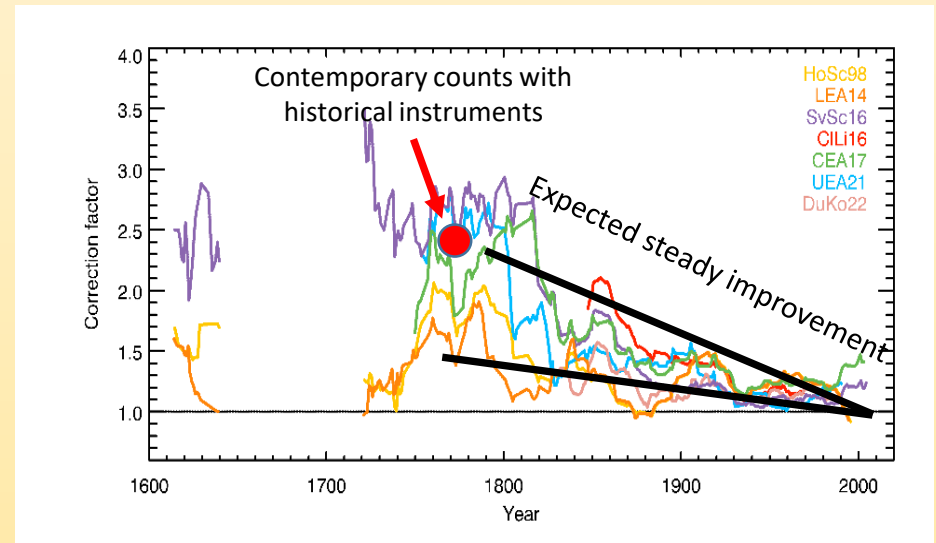
4365/ac24a7



z, Spain

# Benchmarks

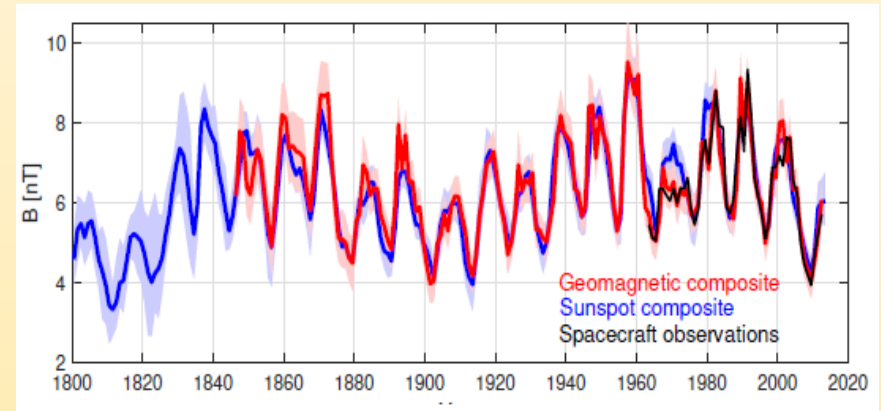
- **Progress in telescope optics:**
  - Ratios between reconstructed and raw uncorrected series
  - Historical optics (*Svalgaard*)
  - Mathematically degraded images (*Karachik, Pevtsov, Nagovitsyn, 2019*)
- **Equivalence  $G_N \leftrightarrow S_N$ :**
  - Same underlying process (magnetic flux emergence)
  - $S_N$  construction is completely independent (pilot station back to 1849)



# Solar activity proxies

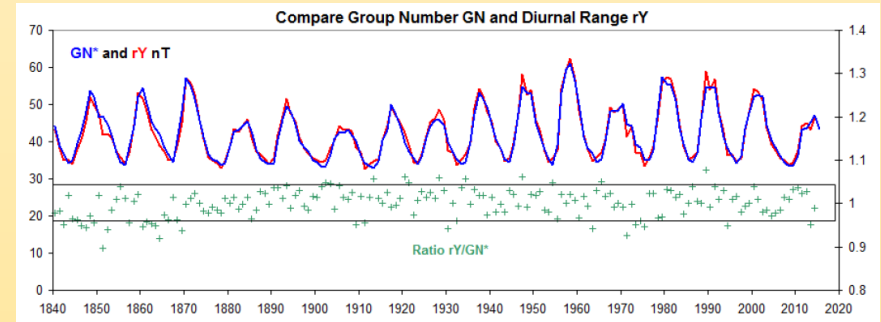
- **Geomagnetic indices:**

- Open magnetic flux in solar wind
- Recent re-calibration (ISSI team) (*Owens et al. 2016*)



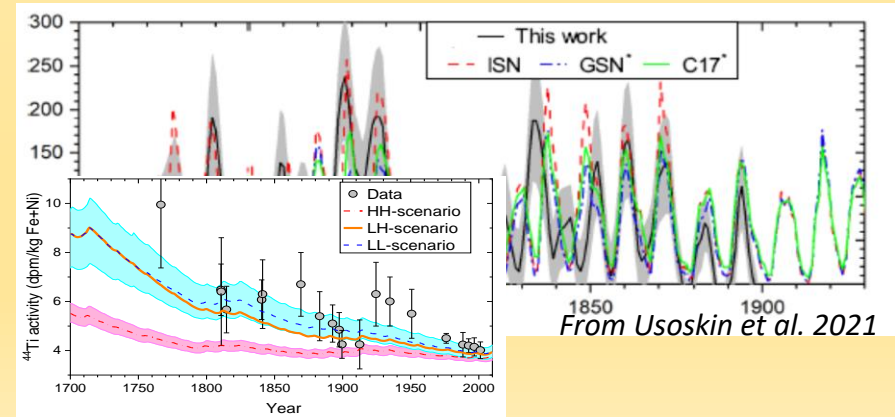
- **Diurnal modulation of the geomagnetic East component  $rY$ :**

- Proxy of solar UV irradiance
- Yearly means 1840-present (*Svalgaard, 2015*)



- **Cosmogenic isotopes ( $^{10}\text{Be}$ ,  $^{14}\text{C}$ ,  $^{44}\text{Ti}$ ):**

- Proxy of solar wind (modulation potential)
- $^{14}\text{C}$  from trees (*Usoskin et al. 2021*)
- $^{44}\text{Ti}$  from meteorites (*Asvestari et al. 2017*)




From Usoskin et al. 2021

# GN benchmark & proxies: overview

	Recons. $G_N$	Optical progress	$S_N$ V2.0	Geomag. Open B	Diurnal rY	Isotopes $^{14}C$ , $^{44}Ti$
<b>HIGH</b>	SvSc2016 CILI16 SN V1/2	<b>BEST</b>	<b>BEST</b>	<b>BEST</b>	<b>BEST</b>	<b>NO</b>
<b>MEDIUM</b>	CEA17 DuKo22 UEA21	<b>FAIR LOW</b>	<b>FAIR LOW</b>	<b>FAIR LOW</b>	<b>FAIR LOW</b>	<b>FAIR HIGH</b>
<b>LOW</b>	HoSc88 LEA14	<b>NO</b>	<b>NO</b>	<b>NO</b>	<b>NO</b>	<b>BEST</b>

- **Low reconstructions are excluded by most benchmarks & proxies**
- **Intermediate reconstructions are mostly compatible but never optimal**
- **Still contradictory diagnostics: subject to revision !**

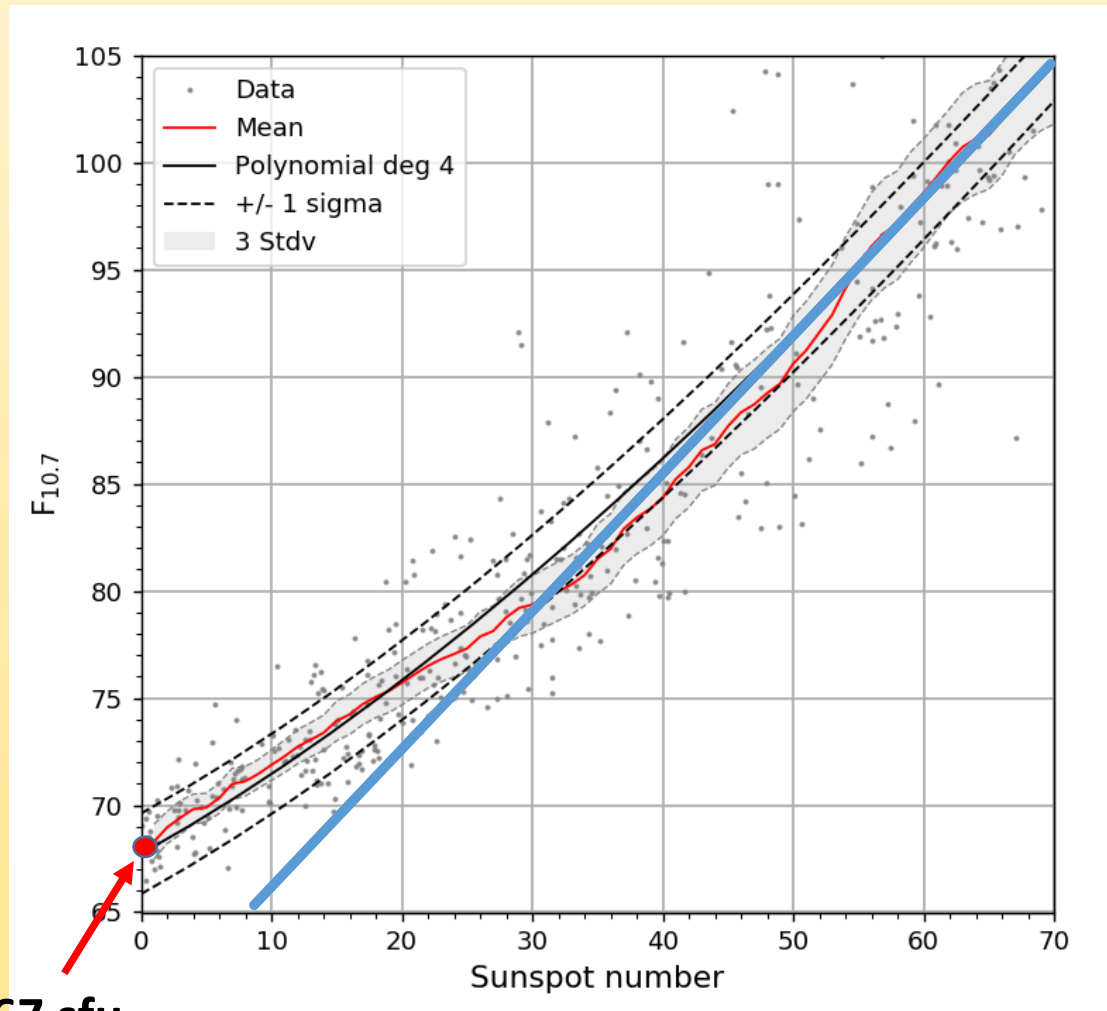
# $G_N$ reconstruction: prospects

- Further **development of the advanced backbone**
  - Single **common data set for testing/benchmarking** all methods
  - Benchmarks: tracking the **progresses in solar activity proxies**
    - *e.g. single solar cycles resolved in  $^{14}C$  isotope records (Usoskin et al. 2021, A&A)*
  - **When everything breaks down!** *All methods are inapplicable during grand minima and when data are too sparse*
    - **Sunspot drawings**= ground truth: e.g. statistics of group types
    - **Local use of proxies** (geomagnetism) to bridge gaps < 10-20 years
  - **Remaining problems common to all methods:**
    1. Hypothesis of **scale uniformity** of individual observers
    2. Effect of **random temporal distribution of sparse data**  
*(cf. Usoskin, Mursula & Kovaltsov 2003, ESAsp)*
  - **Addressed by  $S_N$  uncertainty quantification** *(Mathieu et al. 2019)*
-  **Next step: mutual adaptation of methods for  $S_N \leftrightarrow G_N$**

# $F_{10.7}$ background radio flux: relation with $S_N$

- Past results:
  - Many disagreeing  $S_N - F_{10.7}$  relations
  - No error range
- **4<sup>th</sup> degree polynomial:**
  - Needed for good fit in the low range
  - Polyn. values + errors
- **Linear for  $S_N > 35$**

$$\begin{aligned}\widehat{F}_{10.7} &= 67.73 (\pm 1.13) \\ &+ 0.337(0.056) S_N \\ &+ 3.69 (\pm 0.77) \cdot 10^{-3} S_N^2 \\ &- 1.52 (\pm 0.38) \cdot 10^{-5} S_N^3 \\ &+ 1.33 (\pm 0.62) \cdot 10^{-8} S_N^4\end{aligned}$$



Mean “all-quiet”  $F_{10.7}(0) = 67$  sfu

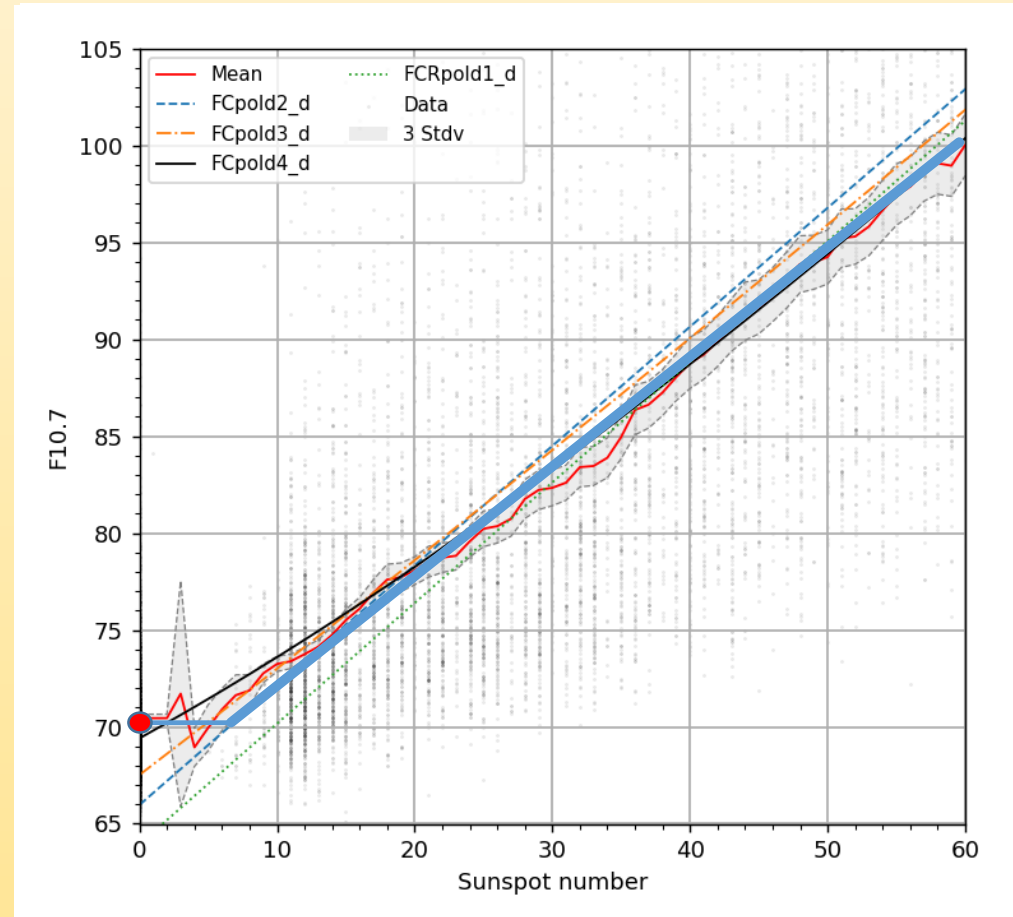
Function of the duration of spotless interval: lowest for  $\sim 30$  day averages

# Model: pure temporal averaging effect

- Raw daily data:
  - Fully linear down to first spot
  - $S_N=0$  is offset (0-11 jump)

$$S_N = 10 N_G + N_S$$

- Synthetic  $F_{10.7}$  series:
  - Linear conversion of actual daily  $S_N$  series to  $F_{10.7}$
  - Monthly averaging



- ➡ Matches the observed low-range non-linearity (also for yearly means)
- ➡ Non-linearity due to the  $S_N=0$  offset point temporally convolved with the frequency of spotless days.

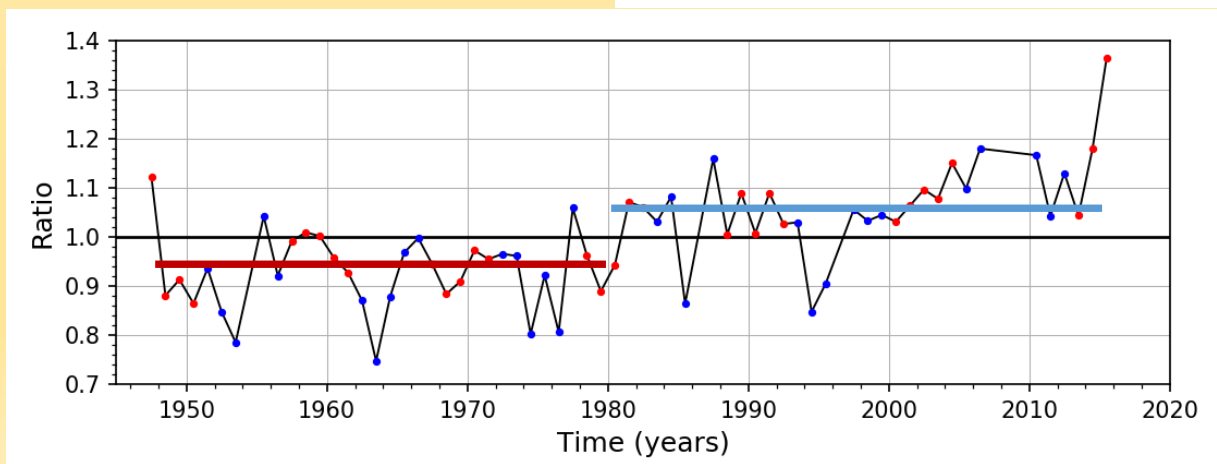
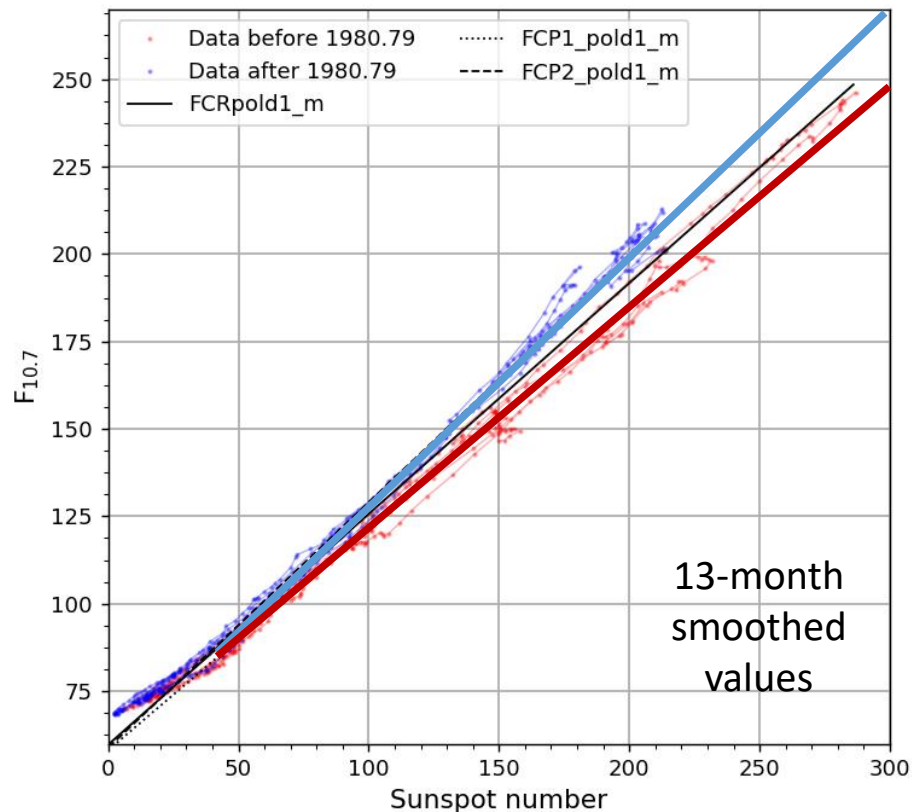
# A sharp jump in 1980

- **Abrupt upward jump in 1980:**
  - Before 1980:  $S = 0.6345 (\pm 0.0066)$
  - After 1980:  $S = 0.7020 (\pm 0.0089)$
  - Ratio:  $1.106 \pm 0.017$  (10.6 %)
  - Time: Dec. 1980 – Jan 1981

➔ **Good global homogeneity of both series before and after the jump**

- Very high linear correlation (V2 better than V1)

➔ **Validation of both series**





# Separate proxies needed for each half-series !

1947-1980

$$\begin{aligned}\hat{F}_{10.7} &= 66.64 (\pm 1.48) \\ &+ 0.366(0.067) S_N \\ &+ 2.59 (\pm 0.86) \cdot 10^{-3} S_N^2 \\ &- 0.99(\pm 0.40) \cdot 10^{-5} S_N^3 \\ &+ 1.33(\pm 0.62) \cdot 10^{-8} S_N^4\end{aligned}$$

1981-present

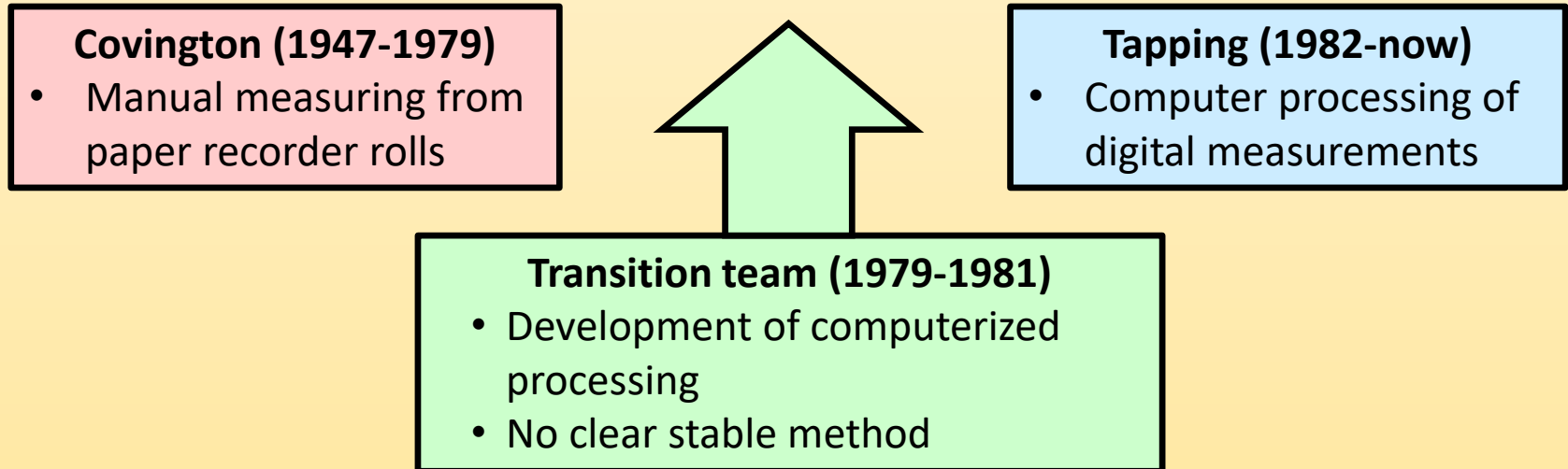
$$\begin{aligned}\hat{F}_{10.7} &= 67.84 (\pm 1.06) \\ &+ 0.386(0.044) S_N \\ &+ 2.86 (\pm 0.45) \cdot 10^{-3} S_N^2 \\ &- 0.73(\pm 0.13) \cdot 10^{-5} S_N^3\end{aligned}$$

Whole series

$$\begin{aligned}\hat{F}_{10.7} &= 67.73 (\pm 1.13) \\ &+ 0.337(0.056) S_N \\ &+ 3.69 (\pm 0.77) \cdot 10^{-3} S_N^2 \\ &- 1.52(\pm 0.38) \cdot 10^{-5} S_N^3 \\ &+ 1.97(\pm 0.60) \cdot 10^{-8} S_N^4\end{aligned}$$

# 1980 jump: retracing the historical cause

- Two main  $F_{10.7}$  construction eras (*non-overlapping*):



- **Processing issue:** unique change of people and method
- **No instrument calibration problem**

Clette, F. (2021), *J. Space Weather and Space Climate*, Vol. 11, id.2, 25 pp.  
DOI: [10.1051/swsc/2020071](https://doi.org/10.1051/swsc/2020071)

# Conclusions

- Multiple topic-focused partnerships: **welcome to join in !**
- Way forward:
  - **Combining methods, apply (only) where they work**
  - **Data uncertainties** become central
- **Next major  $S_N$  update: release 2024**
- Reconstruction of  $S_N$  &  $G_N$  series now a **continuous process**
- Steps towards a formal **version-adoption framework (IAU):**
  - Base community (ISSI Team) > In progress ...
- **A new generation of young sunspot researchers !**
  - Theo, Hisashi, Shreya, Sophie, Victor, etc.



# Stay tuned ....



## World Data Center – SILSO

Sunspot Index and Long-term Solar Observations

<http://sidc.be/silso>



Sunspot Index and Long-term  
Solar Observations

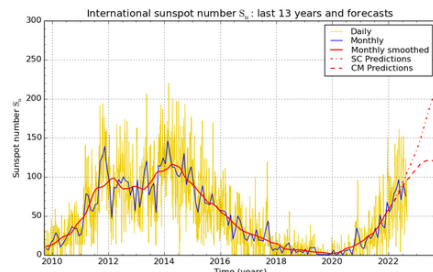
### Menu

- Home
- Data
- Products
- Analyses
- FAQ & News
- Observers
- Contact
- Legal notices
- About

Home Data Products Analyses FAQ & NEWS Observers Contact

World Data Center for the production, preservation and dissemination of the international sunspot number

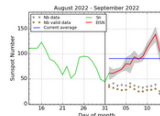
### Sunspot number series: latest update



SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 September 1

### Latest Sunspot Bulletin

#### Daily estimated sunspot number

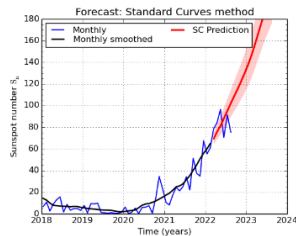


SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 September 1

#### EISN DATA FILES

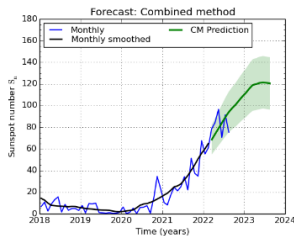
- 10 September : 112
- 11 September : 125
- 12 September : 139
- 13 September : 105

### New extended hemispheric sunspot numbers



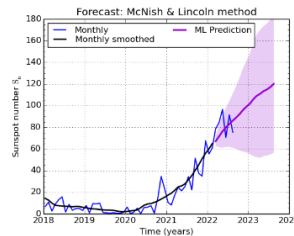
SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 September 1

Standard Curves method (SC)



SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 September 1

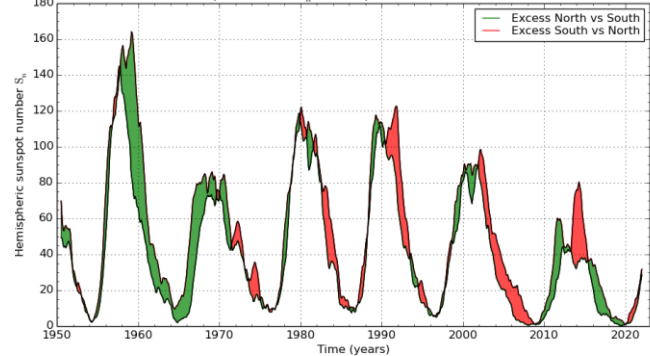
Combined method (CM)



SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 September 1

McNish&Lincoln method (ML)

### International sunspot number $S_i$ ; hemispheric 13-month smoothed numbers



SILSO graphics (<http://sidc.be/silso>) Royal Observatory of Belgium 2022 August 1

